UDC 629.735.33-519 (045)

O. I. Nadsadna

## ROBUST GAIN-SCHEDULED CONTROL FOR UNMANNED AERIAL VEHICLES

Antonov Company, Tupolev Str. 1, 03062, Kyiv, Ukraine E-mail: nadsadna@ukr.net

Absract—The flight dynamics of a modern aircraft are highly nonlinear and vary over the wide flight envelope of the aircraft. This fact makes it difficult for a single controller to achieve the desired closed-loop specifications. This paper considers gain-scheduling successive loop control design for linear parameter-varying system in terms of linear matrix inequalities. The obtained controller guarantees an efficient unmanned aerial vehicle's control under external disturbances within the flight envelope. The design procedure is illustrated by a case study of unmanned aerial vehicle lateral channel control.

Index terms—Gain scheduling; linear matrix inequalities; robustness; unmanned aerial vehicle.

## I. INTRODUCTION

The flight envelope of modern UAVs is expanded constantly [1]. It leads to significant changing of linearized mathematical models of aircraft. Flight control of such UAVs confronts the challenge of high-precision tracking with strong robustness for the entire flight envelope. In this case gain scheduling (GS) control becomes very powerful instrument for increasing of flight control system robustness.

The flight control system explored in this paper consists of a Successive Loop Closure (SLC) baseline controller [2] which can be obtained conveniently by solving linear matrix inequalities (LMI) [3] – [7], [10] with reduced computational complexity. In order to obtain numerical results we consider lateral motion control including roll angle stabilization as the inner loop, heading angle stabilization as the intermediate loop, and the reference track stabilization in the horizontal plane as the outer loop. The model of UAV used in this research is Aerosonde which is supported by Aerosim Matlab Toolbox [9].

# II. ANALYSIS OF RECENT RESEARCH AND PUBLICATIONS

The gain scheduling control problem has been widely developed both from theoretical and practical viewpoints, see, for example, [11], [12]. An effective approach to solve the nonlinear control problem is using gain scheduling with linear parameter-varying (LPV) controller [18]. For example, the parameters of the mathematical model of an aircraft

depend on the altitude and speed (Mach number), which determine the dynamic pressure (DP):  $\overline{q} = \rho v^2/2$ , where  $\rho$  is density of air, kg/m³, v is air speed, m/s. The main advantage of DP, that this parameter is related with both flight altitude and speed values. As far as all entries of the stability and control matrices **A**, **B** could be considered as functions of  $\overline{q}$ :  $\mathbf{A}(\overline{q})$ ,  $\mathbf{B}(\overline{q})$  [13], then for these matrices it is possible to find parameters of the controller from the point of view of robust stability and robust performance for each numerical value of  $\overline{q}$ .

## III. PROBLEM STATEMENT

Let us consider a LPV system in form

$$\begin{cases}
\dot{x}(t) = A(\overline{q})x(t) + B(\overline{q})u(t) + B_{\nu}(\overline{q})v(t), \\
y(t) = C(\overline{q})x(t) + D(\overline{q})u(t),
\end{cases}$$
(1)

where  $x = [\beta, p, r, \varphi, \psi, \tilde{y}]^T$  is the state vector with components: sideslip angle  $\beta$ , roll and yaw rates p, r respectively, and roll and yaw angles  $\varphi, \psi$  and cross-track error  $\tilde{y}$ ;  $u = [\delta_a, \delta_r]^T$  - the control vector with components: the deflection of ailerons and rudder respectively;  $y = [p, r, \varphi, \psi, \tilde{y}, V_{\tilde{y}}]^T$  is the observation vector, where  $V_{\tilde{y}}$  stands for the side velocity;  $\mathbf{A}, \mathbf{B}, \mathbf{C}$  and  $\mathbf{D}$  are the state matrices that depend on parameter DP;  $\mathbf{B}_{\mathbf{v}}$  is the matrix external disturbance.

The block diagram of the UAV lateral motion control system with SLP is shown in Fig. 1 [19].

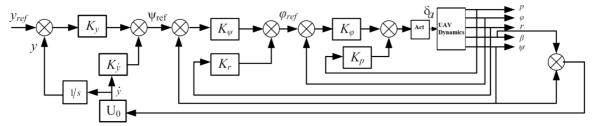


Fig. 1. Block diagram of the UAV lateral motion with successive loop control

It represents 3 successive closed loops with standard PD control laws, so the innermost loop (roll angle control) has control law

$$\delta a(z) = W_{\text{act}}(z) \left( K_{\varphi} \varphi + K_{p} p \right). \tag{2}$$

The same PD control laws are accepted for the yaw angle control (intermediate loop) with coefficients  $K_{\psi}$ ,  $K_{r}$  as well as for the outermost crosstrack error y loop with coefficients  $K_{\tilde{y}}$ ,  $K_{V_{y}}$ .

The output of the outer control law serves as the reference (command) signal to the corresponding inner loop. It is known [2], [8] that in order to suppress sideslip angle  $\beta$  for the coordinated turn execution, the standard washout filter with transfer function

$$W_{wf}(s) = K_{wf} \frac{T_{wf} s}{T_{wf} s + 1},$$

is applied as a local feedback from the yaw rate r sensor to the deflection of rudder  $\delta_r$ . For the sake of the further simplification we neglect the dynamics of this local loop, so we will consider only main contour with single input – deflection of the aileron  $\delta_a$ , as it is shown in the Fig. 1.

The goal of the research is to design a family of local LMI-controllers.

The algorithm of controller design in terms of LMIs was proposed in [5] - [7].

The control law is given by

$$u(t) = -Ky(t) = -KCx(t), \tag{3}$$

where  $\mathbf{K}$  is a constant output feedback gain matrix.

The exogenous disturbances v are restricted by  $L_2$ -norm

$$\left\| v(t) \right\|^2 = \int_0^\infty (v^{\mathsf{T}} v) dt < \infty . \tag{4}$$

 $L_2$ -norm assures disturbance attenuation with a predefined level, v.

**K** matrix minimizes a performance index:

$$J(K) = \int_{0}^{\infty} ||z(t)||^{2} dt = \int_{0}^{\infty} (x^{\mathsf{T}} Q x + u^{\mathsf{T}} R u) dt$$
$$\leq \gamma^{2} \int_{0}^{\infty} v^{\mathsf{T}} v dt, \ \forall v(t) \neq 0,$$

where  $Q \ge 0$ , R > 0 are diagonal matrices, weighting each state and control variables, respectively. Output signal z(t) used for performance evaluation is defined as follows:

$$z = \begin{bmatrix} \sqrt{Q} & 0 \\ 0 & \sqrt{R} \end{bmatrix} \begin{bmatrix} x \\ u \end{bmatrix}.$$

The system  $L_2$  gain is said to be bounded or attenuated by  $\gamma$  if [3], [5], [6], [10]:

$$\int_{0}^{\infty} ||z(t)||^{2} dt = \int_{0}^{\infty} (x^{\mathrm{T}} Q x + u^{\mathrm{T}} R u) dt \le \gamma^{2}.$$

Therefore, it is necessary to find constant output feedback gain matrix K that stabilizes the control plant such that the infinity norm of the transfer function referring exogenous input to performance output z(t) approaches minimum. The minimum  $L_2$ -gain (4) is denoted by  $\gamma^{\bullet}$ .

The output feedback gain matrix **K** could be found by solving the following LMI [5], [6]

$$\begin{bmatrix} PA_i + A_i^{\mathsf{T}} P + Q & P_n B & P_n B_{iv} & 0 \\ B_i^{\mathsf{T}} P & -R & 0 & 0 \\ B_{iv}^{\mathsf{T}} P & 0 & -\gamma^2 I & 0 \\ 0 & 0 & 0 & -R \end{bmatrix} \le 0, \quad (5)$$

where i = 1, ..., N in (5) denotes the set of models associated with scheduled operating conditions within the flight envelope.

The matrices K are:

$$K_{i} = R^{-1}B_{i}^{T}P_{i}Ci^{T}(C_{i}C_{i}^{T})^{-1}$$
.

It is desired to find a family of static output-feedback control gain matrices K such that the system is stable and the  $L_2$  gain is bounded by a prescribed value  $\gamma$ .

## IV. GAIN SCHEDULING CONTROLLER

A gain scheduling control system design takes following steps:

- 1. Choose the operating points or region in the scheduling space, which is defined by flight envelope of UAV. Obtain a plant model for each operating region by linearizing the plant's model in the several equilibrium operating points.
- 2. Design a family of local LMI-controllers for the obtained plant models.
  - 3. Implement a scheduling mechanism.
- 4. Assess the GS closed loop stability and performance.

The block-scheme of a GS-feedback loop is shown on Fig. 2.

The vector of adjustable parameters of the autopilot  $\mathbf{K}$  has the following components:

$$\overline{K}(\overline{q}) = [K_{\varphi}(\overline{q}), K_{p}(\overline{q}), K_{\psi}(\overline{q}), K_{r}(\overline{q}), K_{r}(\overline{q}), K_{v_{z}}(\overline{q})]^{T}.$$
(6)

The objective of linearization scheduling is that the equilibrium family of the controller (6) matches the equilibrium family of the plant (1), such that:

- the closed-loop system still can be tuned appropriately with respect to performance and robustness demands;
- the linearization family of the controller equals the designed family of linear controllers.

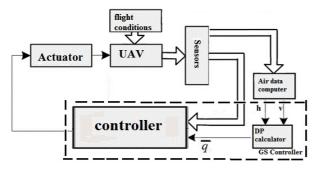


Fig. 2. The block scheme of a hold feedback loop

It was considered the interpolation of the control signals generated by linear interpolation [14].

The model of the atmospheric conditions is a Dryden filter defined by the following transfer functions [15]:

1. Lateral transfer function

$$H_r(s) = \frac{\frac{s}{V}}{1 + \frac{3b}{\pi V}s} \sigma_v \sqrt{\frac{L_v}{\pi V}} \cdot \frac{1 + \sqrt{3} \frac{L_v}{V}s}{\left(1 + \frac{L_v}{V}s\right)^2}$$

2. Vertical transfer function

$$H_{q}(s) = \frac{\frac{s}{V}}{1 + \frac{4b}{\pi V}s} \sigma_{w} \sqrt{\frac{L_{w}}{\pi V}} \cdot \frac{1 + \sqrt{3} \frac{L_{w}}{V}s}{\left(1 + \frac{L_{w}}{V}s\right)^{2}}$$

The variable *b* represents the aircraft wingspan. The variables  $L_v$ ,  $L_w$  represent the turbulence scale lengths. The variables  $\sigma_v$ ,  $\sigma_w$  represent the turbulence intensities.

The performance and robustness indices are possible to estimate after a family of gain-scheduled static output controllers is obtained using proposed approach. Thus, performance is estimated by  $H_2$ -norm of system function with respect to disturbance, whereas the robustness is estimated by  $H_{\infty}$ -norm of the complementary sensitivity function [16].

1. H<sub>2</sub>-norms of system sensitivity function in deterministic case:

$$||H||_{2\text{det}}^n = \sqrt{trace(C_n W_n C_n^{\mathrm{T}})},$$

where  $W_n$  is a controllability gramian and  $C_n$  is a weighting matrix in deterministic.

2. H<sub>2</sub>-of system sensitivity function in stochastic case:

$$||H||_{2st}^n = \sqrt{trace(C_{st}W_{st}C_{st}^T)},$$

where  $W_{\rm st}$  is a controllability gramian and  $C_{\rm st}$  is weighting matrix in stochastic case.

3.  $H_{\infty}$ -norm of the complementary sensitivity function:

$$||H(j\omega)||_{\infty} = \sup_{\omega} \overline{\sigma}(H(j\omega)),$$

where  $\sigma$  is the singular value of complementary sensitivity matrix;  $\overline{\sigma}$  is the maximum singular value on the current frequency.

The block-diagram of the closed-loop system for control of lateral motion is depicted on Fig. 3, where  $\eta$  is white noise vector,  $y_{\rm ref}$  is cross track distance reference signal,  $h_{\rm ADC}$ ,  $V_{T_{\rm ADC}}$  are altitude and true speed measured by Air Data Computer.

The nonlinear model of the Aerosonde is linearized for the range of operating conditions respected to the range of DP from 200 to 650 kg/(ms²) with a granularity of 50 kg/(ms²). The state space matrices **A** and **B** in general form filled with stability and control derivatives are given below [17]:

$$\mathbf{A} = \begin{bmatrix} Y_{\beta} & Y_{p} & Y_{r} - V_{t} & g\cos\theta_{e} & 0 & 0 \\ L_{\beta} & L_{p} & L_{r} & 0 & 0 & 0 \\ N_{\beta} & N_{p} & N_{r} & 0 & 0 & 0 \\ 0 & \frac{\cos\gamma_{e}}{\sin\theta_{e}} & \frac{\sin\gamma_{e}}{\cos\theta_{e}} & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ V_{t} & 0 & 0 & 0 & V_{t} & 0 \end{bmatrix};$$

$$\mathbf{B} = egin{bmatrix} Y_{\delta a} \ L_{\delta a} \ N_{\delta a} \ 0 \ 0 \ 0 \end{bmatrix},$$

where 
$$Y_{\beta} = \frac{\overline{q}S}{m} C_{Y_{\beta}}$$
;  $Y_{p} = \frac{\overline{q}Sb}{2mV_{t}} C_{Y_{p}}$ ;  $Y_{r} = \frac{\overline{q}Sb}{2mV_{t}} C_{Y_{r}}$ ;

$$\begin{split} & Y_{\delta a} = \frac{\overline{q}S}{m} C_{Y_{\delta a}}; \qquad L_{\beta} = \frac{\overline{q}Sb}{J'_{X}} C_{l_{p}}; \qquad L_{p} = \frac{\overline{q}Sb}{J'_{X}} 2V_{t} C_{l_{p}}; \\ & L_{r} = \frac{\overline{q}Sb}{J'_{X}} 2V_{t}; \qquad L_{r} = \frac{\overline{q}Sb}{J'_{X}} 2V_{t} C_{l_{r}}; \qquad L_{\delta a} = \frac{\overline{q}Sb}{J'_{X}} C_{l_{\delta a}}; \\ & L_{\beta} = \frac{\overline{q}Sb}{J'_{Z}} C_{N_{\beta}}; \qquad N_{p} = \frac{\overline{q}Sb}{J'_{Z}} 2V_{t} C_{N_{p}}; \qquad N_{r} = \frac{\overline{q}Sb}{J'_{Z}} C_{N_{\delta a}}; \end{split}$$

 $\theta = \theta_e$ ,  $\gamma = \gamma_e$  are equilibrium (steady-state) conditions,  $J_X$ ,  $J_Z$  are moments of inertia.

As seen from the description of space matrices coefficients, the aircraft flight dynamic depends on DP value. The LPV controller model is a finite set of linear controller models obtained for the operating grid of DP values. The set of linear controllers are shown in Table I. Linear interpolation on a set of data points  $(K_{\varphi_i}, q_i), (K_{p_i}, q_i), (K_{r_i}, q_i), (K_{\widetilde{y}_i}, q_i), (K_{W_{\widetilde{y}_i}}, q_i)$  is defined as the concatenation of linear

interpolants between each pair of data points.

Table II reflects standard deviations of the UAV outputs in a stochastic case of parametrically perturbed model with the static output feedback controller in a control loop.

As it follows from this table r.m.s. of state variables in the stochastic case are varying in reasonable limits. Performance and robustness indices are shown in Table III.

The low variation of the values of  $H_{\infty}$ -norms proves the high degree of the system robustness. Basing on the results of the  $H_2$ -norm values, it is possible to conclude that the norms vary in small ranges. Their close values give a possibility to state that the efficiency of the closed-loop system is held at the desired level.

To illustrate the applicability of our approach, we present numerical examples.

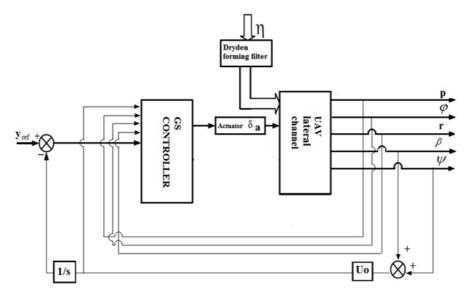


Fig. 3. Block diagram of the UAV lateral motion

TABLE I
CONTROLLER GAINS

$\mathbf{DP}, \frac{\mathbf{kg} \cdot \mathbf{m}}{\mathbf{s}^2}$	$\textbf{Controller gains } \overline{K}(\overline{q}) = [K_{\tilde{y}}(\overline{q}), K_{p}(\overline{q}), K_{r}(\overline{q}), K_{\varphi}(\overline{q}), K_{\psi}(\overline{q}), K_{V_{\tilde{y}}}(\overline{q})]^{\mathrm{T}}$
<200	[0.0762 5.5182 2.8793 1.4693 0.1947 1.162];
250	[0.0778 5.4542 3.0032 1.3543 0.186 1.1596];
300	[0.0774 5.8683 3.038 1.3825 0.1042 1.0186];
350	[0.0802 6.997 3.7347 1.498 0.1626 1.1449];
400	[0.0876 6.727 3.0362 1.2665 0.192 1.1604];
450	[0.0897 5.9078 2.9427 1.85 0.1609 1.144];
500	[0.0921 4.431 2.971 1.5006 0.2052 1.146];
550	[0.0904 6.284 3.2591 1.3928 0.190 1.1489];
600	[0.1069 8.9126 3.379 1.345 0.3529 1.1508];
650>	[0.103 9.2528 3.1936 1.379 0.342 1.1492];

kg⋅m	Standart deviation					
<b>DP</b> , $\frac{\text{kg} \cdot \text{m}}{\text{s}^2}$	$\sigma_{\beta}$ , deg	$\sigma_p$ , deg/s	$\sigma_r$ , deg/s	$\sigma_{_{\phi}}$ , deg	$\sigma_{\psi}$ , deg	$\sigma_{\delta a}$ , deg
200	0.0892	0.1214	0.0206	0.0546	0.1873	0.0681
250	0.0873	0.1255	0.019	0.0519	0.1964	0.0764
300	0.0727	0.1442	0.0354	0.0958	0.4691	0.0742
350	0.09	0.1675	0.025	0.0836	0.3326	0.0867
400	0.0694	0.1678	0.0407	0.1272	0.4528	0.0787
450	0.1079	0.154	0.0218	0.0305	0.0944	0.0601
500	0.1094	0.1653	0.025	0.0467	0.1199	0.0587
550	0.1017	0.1461	0.0239	0.0404	0.1105	0.0529
600	0.1108	0.2141	0.027	0.0674	0.1735	0.0936
650	0.108	0.2137	0.0269	0.0612	0.1656	0.0919

TABLE II STANDARD DEVIATIONS

TABLE III PERFORMANCE INDICES

DP,	H <sub>2</sub> -norm	H∞-norm	
kg⋅m	Deterministic	Stochastic	
$-s^2$	case	case	
<200	0.0437	0.1135	0.566
250	0.1028	0.3901	0.8288
300	0.2384	0.8646	0.8723
350	0.0769	0.3586	0.7574
400	0.2458	0.5277	0.6940
450	0.017	0.0271	0.6226
500	0.0457	0.0269	0.5774
550	0.0454	0.016	0.5299
600	0.0192	0.0314	0.599
650>	0.0184	0.0185	0.6037

The flight condition 1: flight altitude is 200 m, speed is 19 m/s, dynamic pressure is 216 kg·m/s<sup>2</sup>.

$$\mathbf{A_1} = \begin{bmatrix} -0.532 & 2.234 & -18.867 & 9.719 & 0 & 0 \\ -3.471 & -17.0531 & 8.207 & 0 & 0 & 0 \\ 0.562 & -2.212 & -0.8578 & 0 & 0 & 0 \\ 0 & 1 & 0.1184 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 19 & 0 & 0 & 0 & 19 & 0 \end{bmatrix},$$

$$\mathbf{B_1} = \begin{bmatrix} -0.854 \\ -75.009 \\ -2.9575 \\ 0 \\ 0 \\ 0 \end{bmatrix}.$$

The flight condition 2: flight altitude is 2050 m and speed is 30 m/s, dynamic pressure is  $478 \text{ kg/m/s}^2$ .

$$\mathbf{A_2} = \begin{bmatrix} -0.537 & -1.67 & -29.9538 & 9.809 & 0 & 0 \\ -4.455 & -21.639 & 10.417 & 0 & 0 & 0 \\ 0.7507 & -2.84 & -1.15 & 0 & 0 & 0 \\ 0 & 1 & 0.056 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 30 & 0 & 0 & 0 & 30 & 0 \end{bmatrix}$$

$$\mathbf{B_2} = \begin{bmatrix} -1.377 \\ -150.455 \\ -5.716 \\ 0 \\ 0 \\ 0 \end{bmatrix}.$$

The flight condition 3: flight altitude is 1460 m, speed is 35 m/s, dynamic pressure is 651 kg m/s<sup>2</sup>.

$$\mathbf{A_1} = \begin{bmatrix} -0.532 & 2.234 & -18.867 & 9.719 & 0 & 0 \\ -3.471 & -17.0531 & 8.207 & 0 & 0 & 0 \\ 0.562 & -2.212 & -0.8578 & 0 & 0 & 0 \\ 0 & 1 & 0.1184 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 19 & 0 & 0 & 0 & 19 & 0 \end{bmatrix}, \quad \mathbf{A_3} = \begin{bmatrix} -0.663 & 0.8345 & -34.99 & 9.803 & 0 & 0 \\ -5.52 & -26.827 & 12.914 & 0 & 0 & 0 \\ 0.93 & -3.521 & -1.425 & 0 & 0 & 0 \\ 0 & 1 & 0.0238 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0238 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 35 & 0 & 0 & 0 & 35 & 0 \end{bmatrix}$$

$$\mathbf{B_3} = \begin{bmatrix} -1.991 \\ -217.61 \\ -8.268 \\ 0 \\ 0 \\ 0 \end{bmatrix}.$$

Transient processes in nominal and parametrically perturbed system, which were simulated taking into account the influence of the random wind, for the input step function  $\tilde{y}_{ref} = 20$  m are shown in Fig. 4.

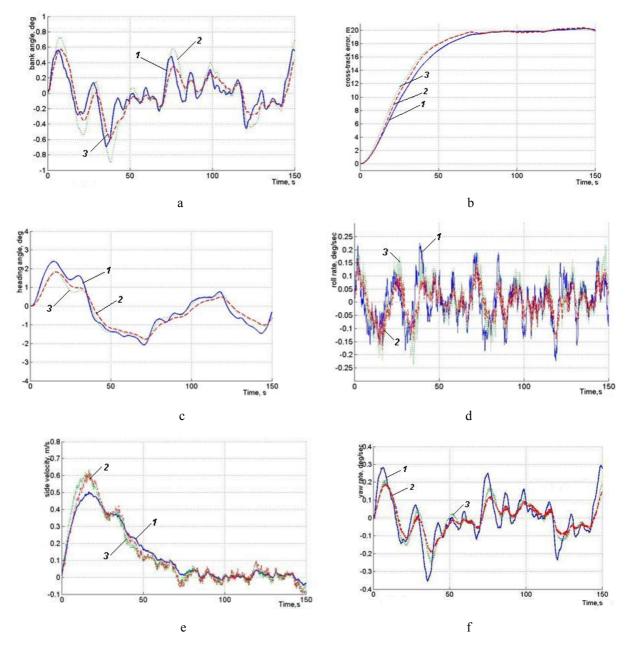


Fig. 4. Simulation results for lateral channel of the UAV in the presence of external disturbances (flight condition 1 is the *solid line*; the flight condition; 2 is *dash line*; the flight condition 3 is *dot line*): (a) is bank angle; (b) is cross-track error; (c) is heading angle; (d) is roll rate; (e) is side velocity; (f) is yaw rate

From the shown below graphs it is evident that results are quite satisfying. Deflections of UAV angular characteristics are possible from the practical point of view. The cross-track value is held at the reference signal  $y_{\text{ref}} = 20$  m with acceptable deflections. These figures along with numerical results, represented in Tables II, III show that desired robustness-performance trade-off is achieved. It can be seen that the handling quality of the nominal and the perturbed models are satisfied.

## V. CONCLUSION

The work presented in this paper was motivated by an UAV with a wide flight envelope. Such vehicles have large parametric variations in the presence of uncertainties. The article presents a procedure of robust GS controller design. The flight control system consists of a SLC baseline controller which can be obtained conveniently by solving LMIs. The method is relatively easy to apply owing to the availability of UAV's computational tools.

The flight envelope of the UAV refers to the capabilities of operating ranges in terms of speed and altitude. The dynamic pressure as function of altitude and speed was proposed as a simple gain scheduled tool for controller design.

The effectiveness of the proposed methods for designing flight controllers is verified and validated through the dynamic model in Matlab Simulink environment of the Aerosonde UAV. However, the proposed methods are also applicable to a general class of conventional aircrafts.

#### **ACKNOWLEDGMENT**

In addition, author highly appreciates Professor A. A. Tunik in helping to provide the research.

## REFERENCES

- [1] R. Austin, *Unmanned Aircraft Systems: UAVS Design, Development and Deployment*, John Wiley & Sons Ltd, Chichester, UK, 2010, 332 p.
- [2] R. W. Beard, and T. W. McLain, *Small Unmanned Aircraft. Theory and Practice*, Princeton University Press, Princeton, NJ, 2012, 300 p.
- [3] O. P. Basanets, A. A. Tunik, and M. M. Komnatska, "LMI-based static output feedback design for rotating solid body", presented at *I-st Intern.Conf. Methods and Systems of Navigation and Motion Control*, Kyiv, 2010, pp. 88–90.
- [4] S. Boyd, L. El. Ghaoui, E. Feron, and V. Balakrishnan, *Linear matrix inequalities in system and control theory*, Philadelphia: PA SIAM, 1994, 205 p.
- [5] J. Gadewadikar, F. Lewis, and M. Abu-Khalaf, "Necessary and sufficient conditions for H-infinity static output feedback control," *Journal of Guidance*, *Control and Dynamics*, vol. 29, pp. 915–921, 2006.
- [6] J. Gadewadikar, and F. Lewis, "Aircraft flight controller tracking design using H-infinity static output-feedback," *Transactions of the Institute of Measurement and Control*, vol. 28, no. 8, pp. 429–440, 2006.
- [7] M. M. Komnatska, "Flight control system design VIA LMI-approach," *Electronics and Control Systems*, no. 3(37), pp. 49–52, 2013
- [8] D. McLean, *Automatic Flight Control Systems*, Prentice Hall, NY, 1990, 593 p.
- [9] J. A. Curry, J. Maslanik, G. Holland, and J. Pinto,

- Application of Aerosonde in the Arctic "American Meteorological Society", pp. 1855–1861, 2004.
- [10] V. L. Syrmos, C. Abdallah, and P. Dorato, "Static output feedback: a survey." In *Proc. of 33rd IEEE Conference on Decision and Control*, Orlando, FL, 1997, pp. 837–842.
- [11] X.Chen, J. Song and G. Cai, "Robust gain-scheduled autopilot design with LPV reference model for portable missile", presented at *IEEE Aerospace Conference*, Montana, 2012, pp. 1–10.
- [12] J. W. Rugh and S. J. Shamma, "Research on gain scheduling", *Automatica*, vol. 36, pp. 1401–1425, 2000.
- [13] R. W. Beard and T. W. Randal, *Small Unmanned Aircraft: Theory and Practice*. Princeton: Princeton University Press, 317 p.
- [14] V. Saeed Vaseghi, Advanced Digital Signal Processing and Noise Reduction, Second Edition, John Wiley & Sons. 2000, pp. 297–330.
- [15]M. O. Rauw, A Simulink Toolbox for Flight Dynamics and Control Analysis, oct 11, 2000, 263 p.
- [16] O. O. Abramovich, and A. A. Tunik, "Multi-Model Approach to Parametric Robust Optimization of Digital Flight Control Systems", *Journal of Automation and Information Sciences*, Begell House Inc., no. 36(3), pp. 25–34, 2004.
- [17] R. W. Beard and T. W. Randal, *Small Unmanned Aircraft: Theory and Practice*. Princeton: Princeton University Press, 317 p.
- [18] Arnar Hjartarson, Peter Seiler, and Gary J. Balas "LPV analysis of a gain scheduled control for an aeroelastic aircraft", presented at 2014 American Control Conference, Portland, OR, 2014, pp. 3778–3783
- [19] A. A. Tunik and M. M. Komnatska, "On structures of combined uav flight control systems with elements of fuzzy logics", *Electronics and Control Systems*, no. 3(41), pp. 20–28, 2014.

Received February 09, 2016

## Nadsadna Olga. Postgraduate student.

Aircraft Control Systems Department, National Aviation University, Kyiv, Ukraine.

Engineer-researcher ANTONOV Company, Kyiv, Ukraine.

Education: National Aviation University, Kyiv, Ukraine (2012).

Research area: control theory and its application.

Publications: 12.

E-mail: nadsadna@ukr.net

## О. І. Надсадна. Робастна система керування беспілотним літальнім апаратом з програмним забезпеченням коефіцієнтів підсилення

Льотна динаміка сучасного літака, яка характеризується високим рівнем нелінійності і варіюється в широкому робочому діапазоні експлуатації об'єкта, ускладнює завдання забезпечення необхідних характеристик зворотного зв'язку з простим регулятором. Розглянуто синтез регулятора з програмним забезпеченням коефіцієнтів посилення для системи із змінними параметрами за допомогою апарату лінійних матричних нерівностей.

Отриманий регулятор гарантує ефективне керування безпілотним літальним апаратом під впливом зовнішніх обурень в робочому діапазоні експлуатації об'єкту. Процедура синтезу проілюстрована на прикладі бічного каналу безпілотного літального апарату.

**Ключові слова:** програмне забезпечення коефіцієнтів підсилення; лінійні матричні нерівності; робастність; безпілотний літальний апарат.

## Надсадна Ольга. Аспірант.

Кафедра систем управління літальних апаратів, Національний авіаційний університет, Київ, Україна.

Інженер-дослідник, ДП «Антонов», Київ, Україна.

Освіта: Національний авіаційний університет, Київ, Україна (2012).

Напрям наукової діяльності: теорія автоматичного керування та її застосування.

Кількість публікацій: 12. E-mail: nadsadna@ukr.net

# О. И. Надсадная. Робастная система управления беспилотным летательным аппаратом с программным обеспечением коэффициентов усиления

Летная динамика современного самолета, которая характеризуется высоким уровнем нелинейности и варьируется в широком рабочем диапазоне эксплуатации объекта, усложняет задачу обеспечения необходимых характеристик обратной связи с простым регулятором. Рассмотрен синтез регулятора с программным обеспечением коэффициентов усиления для системы с переменными параметрами с помощью аппарата линейных матричных неравенств. Полученный регулятор гарантирует эффективное управление беспилотным летательным аппаратом под воздействием внешних возмущений в рабочем диапазоне эксплуатации объекта. Процедура синтеза приведена на примере бокового канала беспилотного летательного аппарата.

**Ключевые слова:** программное обеспечение коэффициентов усиления; линейные матричные неравенства; робастность; беспилотный летательный аппарат.